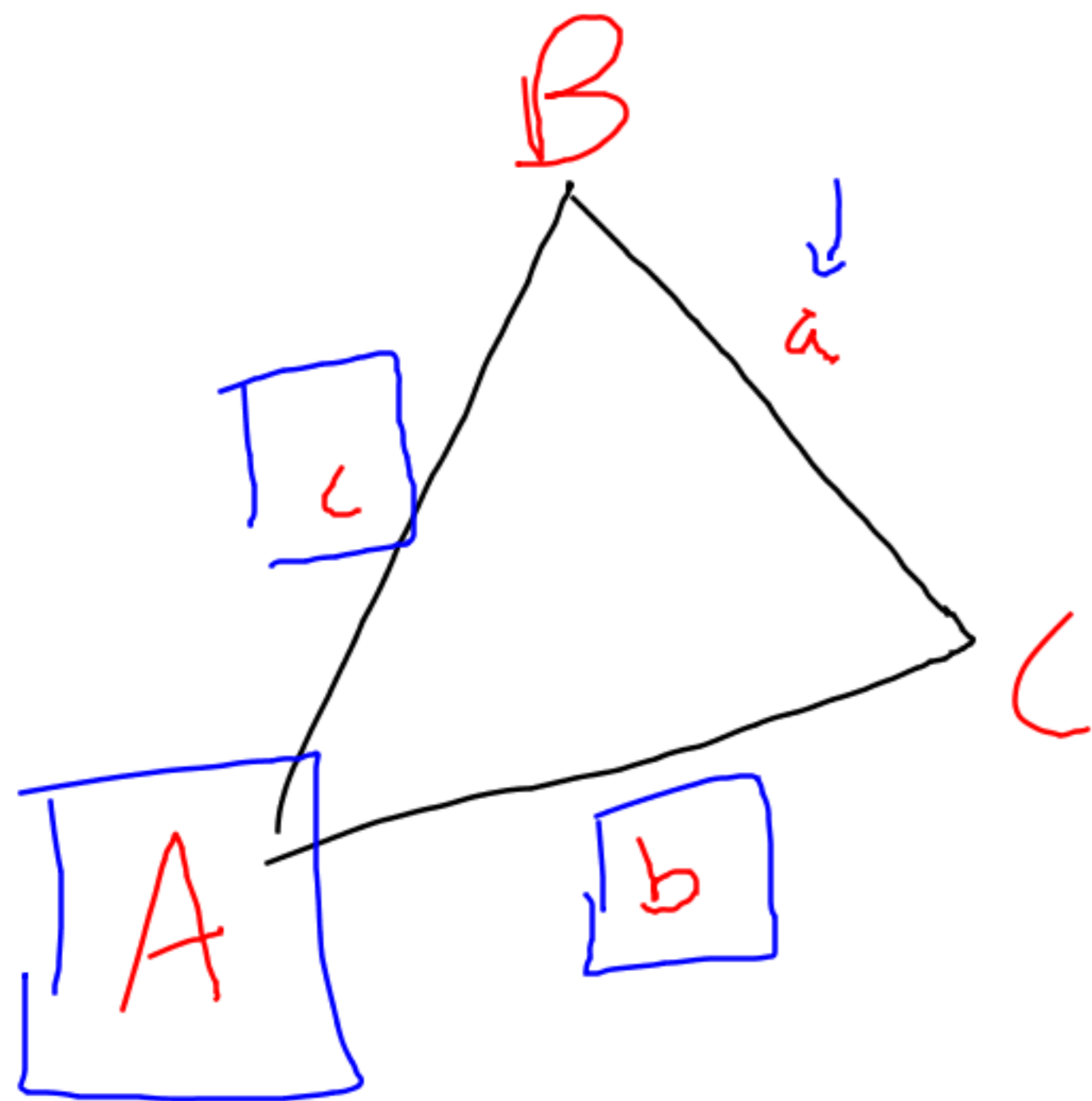


# Mathematics 11C

## 1.4 – The Cosine Law

Mr. D. Hagen



$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$b^2 = a^2 + c^2 - 2ac \cos B$$

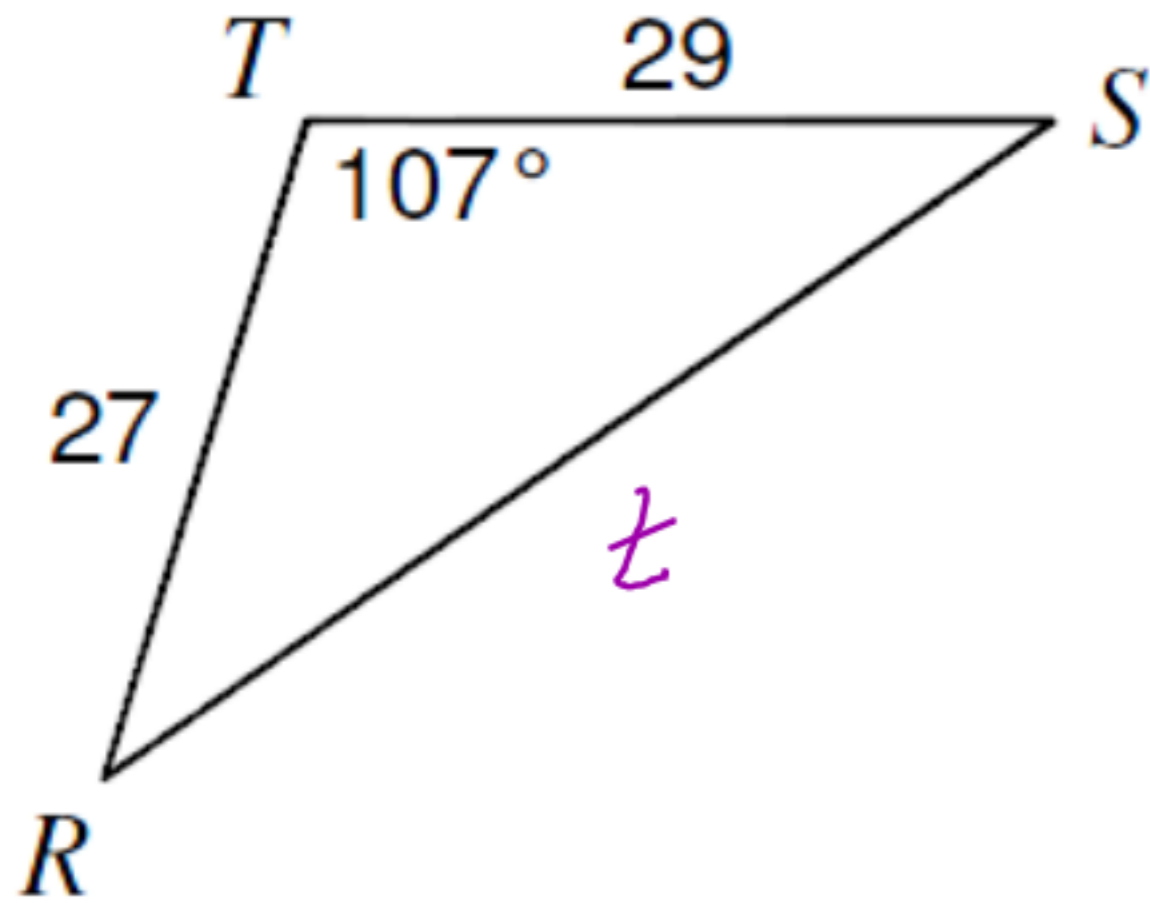
$$c^2 = a^2 + b^2 - 2ab \cos C$$

- 2 sides and the angle that joins them together

or

- all 3 sides

1) Find ~~RS~~  $t$



$$t^2 = r^2 + s^2 - 2rs \cos T$$

$$t^2 = 29^2 + 27^2 - 2(29)(27) \cos 107$$

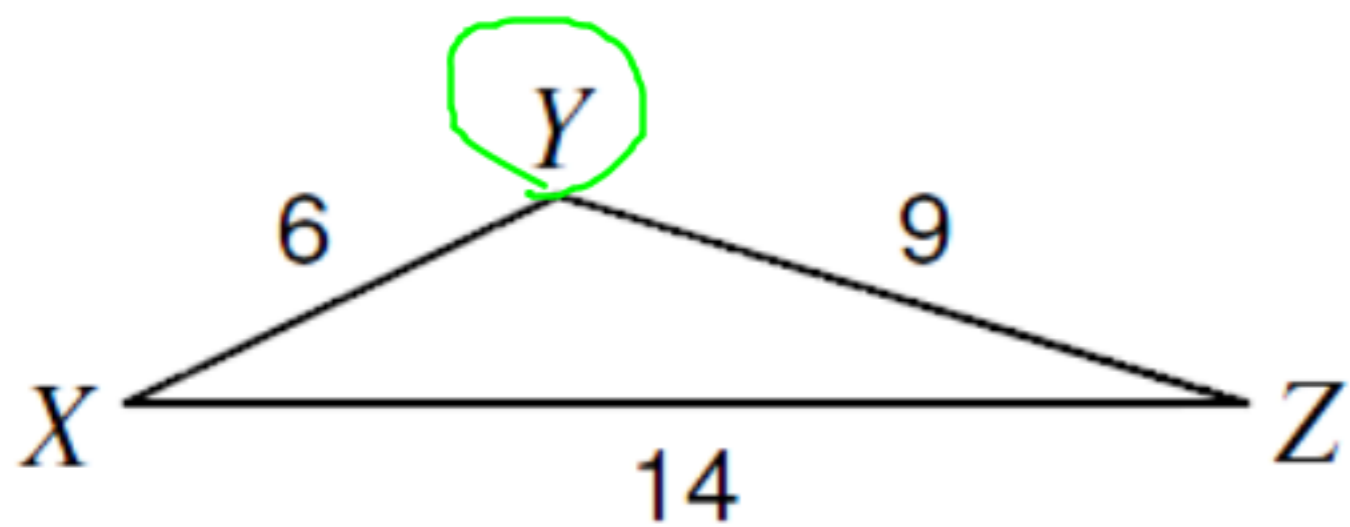
$-457.85$

$$t^2 = 841 + 729 + 457.85$$

$$\sqrt{t^2} = \sqrt{2027.85}$$

$$t = 45$$

2) Find  $m\angle Y$



$$Y^2 = X^2 + Z^2 - 2XZ \cos Y$$

$$14^2 = 9^2 + 6^2 - 2(9)(6) \cos Y$$

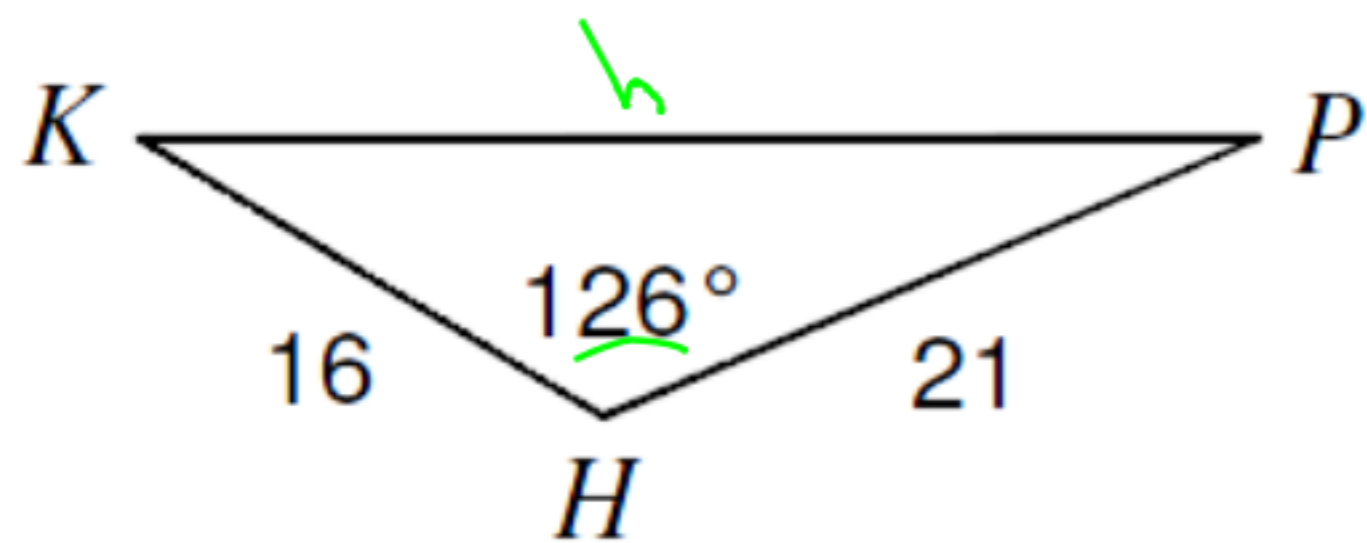
$$196 = 81 + 36 - 108 \cos Y$$

$$79 = \frac{-108 \cos Y}{-108}$$

$$-0.7315 = \cos Y$$

$$\cos^{-1}(-0.7315) = Y = 137^\circ$$

3) Solve



$$\angle K = 31^\circ \quad k = 21$$

$$\angle P = 23^\circ \quad p = 16$$

$$\angle H = 126^\circ \quad \leftrightarrow \quad h = 33$$

$$h^2 = 16^2 + 21^2 - 2(16)(21)\cos 126$$

$$h^2 = 256 + 441 + 395$$

$$\sqrt{h^2} = \sqrt{1092}$$

$$h = 33$$

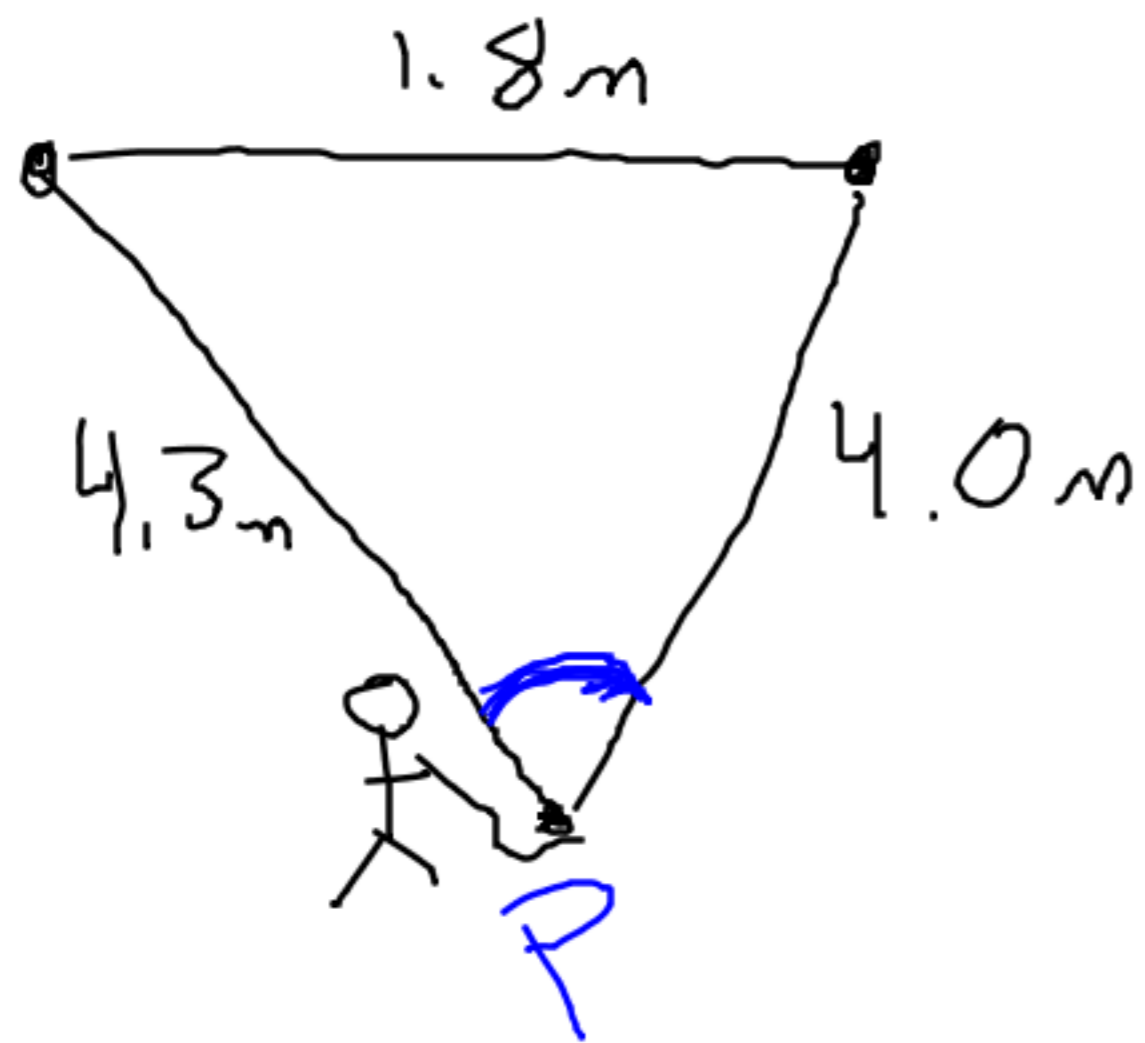
$$\frac{\sin P}{16} = \frac{\sin 126}{33}$$

$$\sin P = 0.3923$$

$$P = \sin^{-1}(0.3923)$$

$$P = 23^\circ$$

The posts of a hockey net are 1.8 m apart. A player tries to score a goal by shooting the puck along the ice from a point that is 4.3 m from one goalpost and 4.0 m from the other goalpost. Determine the measure of the angle that the puck makes with both goalposts.



$$1.8^2 = 4^2 + 4.3^2 - 2(4)(4.3)\cos P$$
$$3.24 = 16 + 18.49 - 34.4\cos P$$
$$\underline{-31.25} = \underline{-34.4\cos P}$$

$$0.9084 = \cos P$$

$$\cos^{-1}(0.9084) = P = 25^\circ$$